# Swelling of Polyelectrolyte Networks with Brush-like Strands

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# **Charged Polymers and Biopolymers**

**Polyelectrolytes** – polymers with positively or negatively charged groups





Extracellular Matrix Drug Delivery Disposable Diapers

# **Balancing Network Elasticity and Interactions**

 $F_{net} = F_{elastic} + F_{osmotic}$ 

Equilibrium swelling volume is set by

$$\frac{\partial F_{elastic}}{\partial V} + \frac{\partial F_{osmotic}}{\partial V} = 0$$

$$\frac{\partial F_{elastic}}{\partial V} = Q^{-1/3}G(Q) = Q^{-1/3}\frac{G_{dr}}{3}\left(1 + 2\left(1 - \frac{\beta I_1(Q)}{3}\right)^{-2}\right)$$

$$-\frac{\partial F_{osmotic}}{\partial V} = \pi(Q) = \begin{cases} \frac{k_B T}{v}\left(\tau \frac{Q^{-2}}{2} + \frac{Q^{-3}}{3}\right) & \text{neutral} \\ P_p - P_s & \text{charged} \end{cases}$$

$$G(Q) = Q^{1/3}\pi(Q)$$





# Nonlinear Shear Modulus

• Stretch the sample to obtain the stressstrain curve. Translate this data to the nonlinear shear modulus using

$$G(I_1) = \frac{\sigma_{true}(\lambda)}{\lambda^2 - \lambda^{-1}}$$
 and  $I_1 = \lambda^2 + 2\lambda^{-1}$ 

• Swell the sample to obtain an equilibrium swelling ratio *Q*. Translate this to the first invariant using

$$I_1(Q) = 3Q^{2/3}$$

• Either fit the stress-strain data or interpolate the data to find G(Q).

$$G(I_1) = \frac{G_{dr}}{3} \left( 1 + 2\left(1 - \frac{\beta I_1}{3}\right)^{-2} \right)$$



# Neutral Bottlebrush Swelling



# Crosslinked Brush-like Chains $U_{LJ}(r) = \begin{cases} 4\varepsilon_{LJ} \left[ \left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^{6} - \left(\frac{\sigma}{r_{cut}}\right)^{12} + \left(\frac{\sigma}{r_{cut}}\right)^{6} \right] & r \le r_{cut} \\ 0 & r > r_{cut} \end{cases}$

$$U_{FENE}(r) = -\frac{K}{2} R_{max}^2 \ln\left[1 - \left(\frac{r^2}{R_{max}^2}\right)\right] + 4\varepsilon_{LJ} \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6\right] + \varepsilon_{LJ}$$

$$\sigma = 1.0 \qquad K = 30k_BT/\sigma^2$$
  

$$r_{cut} = 2^{1/6} \qquad R_{max} = 1.5\sigma$$

Effective bending potential due to side chain interaction Isobaric-isothermal (NPT) ensemble:  $P = 0.0k_BT/\sigma^3$ Polymer architecture range

$$0.5 \le n_g \le 16$$
  $2 \le n_{sc} \le 32$  5

# Simulations of Neutral Bottlebrush Swelling



# Charged Systems

#### Coulombic potential $U_{Coul}(r_{ij}) = k_B T \frac{l_B q_i q_j}{r_{ij}}$ - Bjerrum length $l_B = \frac{e^2}{\epsilon k_B T} = \sigma$

#### Linear Salt Solutions

LJ potential + FENE bonds Fraction of charged monomers f = 1



#### **Bottlebrush Networks**

The same systems as the neutral networks, with positive charges added every 1, 2, or 4 side chain monomers, and counterions added for system neutrality



# **Osmotic Pressure**



Polymers 2014, 6, 1897-1913

# **Comparison of Charged and Neutral Networks**

$$\pi(Q) = Q^{-1/3} G(Q)$$
$$\frac{G(Q)}{\rho k_B T} = f Q^{-2/3} + B Q^{-8/3}$$
$$Q^{2/3} \frac{G(Q)}{\rho k_B T} = f + B Q^{-2}$$



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# Conclusions

- Network swelling is the result of an interplay between osmotic pressure and nonlinear elasticity.
- In neutral systems, osmotic pressure is driven by particle-solvent interaction, while in charged systems it is dominated by osmotic pressure of counterions.
- Our analysis has shown that it is necessary to use melt-state stress-strain data to properly analyze network swelling properties for both charged and neutral systems.



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# Acknowledgements









Dr. Jan-Michael Carrillo (ORNL)

Dr. Heyi Liang (Univ. of Chicago)

Dr. Zilu Wang

Prof. Andrey V. Dobrynin



National Science Foundation (DMR 1921923)



### **Pressure Dependence**



Polymers 2014, 6, 1897-1913