

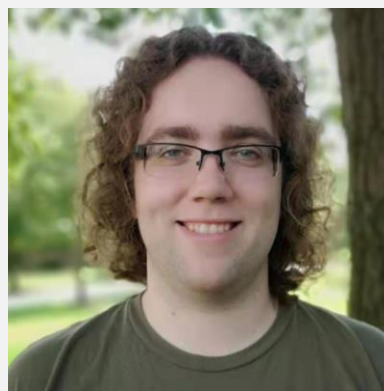
THE UNIVERSITY  
of NORTH CAROLINA  
at CHAPEL HILL

# How to measure the effects of solvents and charged groups on polymer excluded volume and Kuhn length

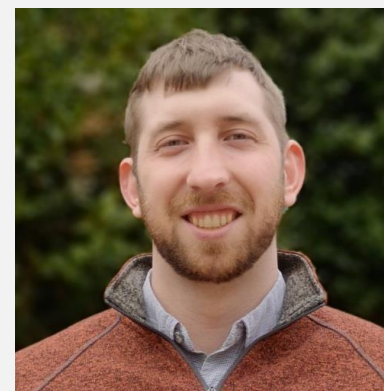
Presented by Michael Jacobs



Andrey V. Dobrynin



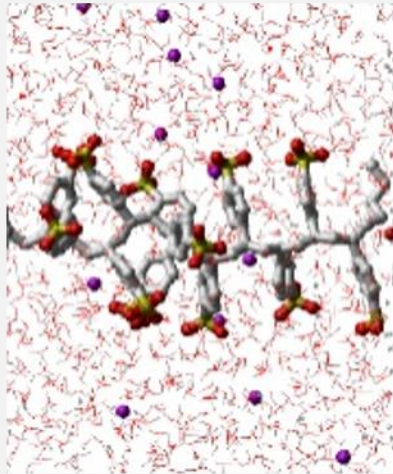
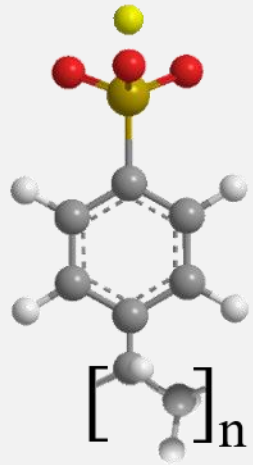
Michael Jacobs



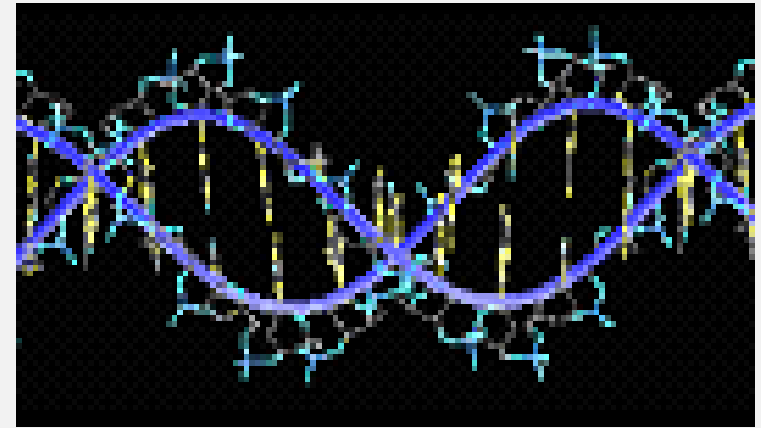
Ryan Sayko

# Polyelectrolytes

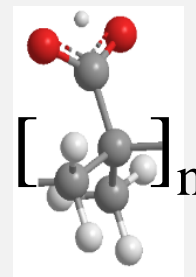
Sodium Poly(styrene sulfonate) (NaPSS)



DNA

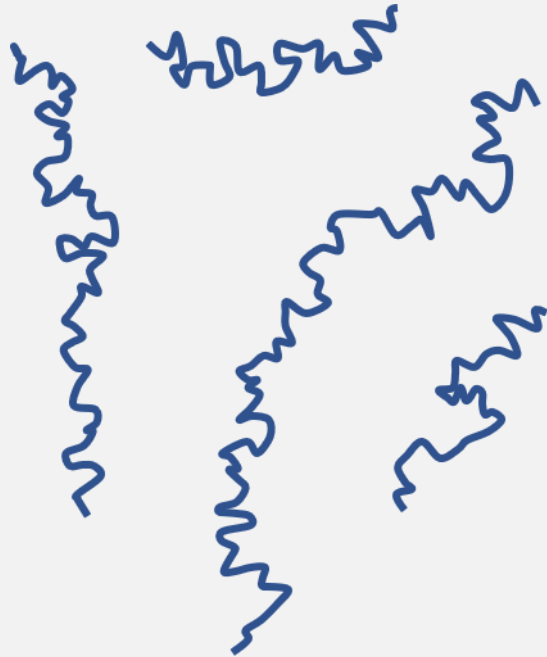


Poly(methacrylic acid)



# Church of the Holy Blob

## Chains in Semidilute Solutions



Chain Size:

$$R = \xi (N/g)^{0.5}$$

Correlation Length (Blob):

$$\xi = D_e g / g_e = l g / B_{pe}$$

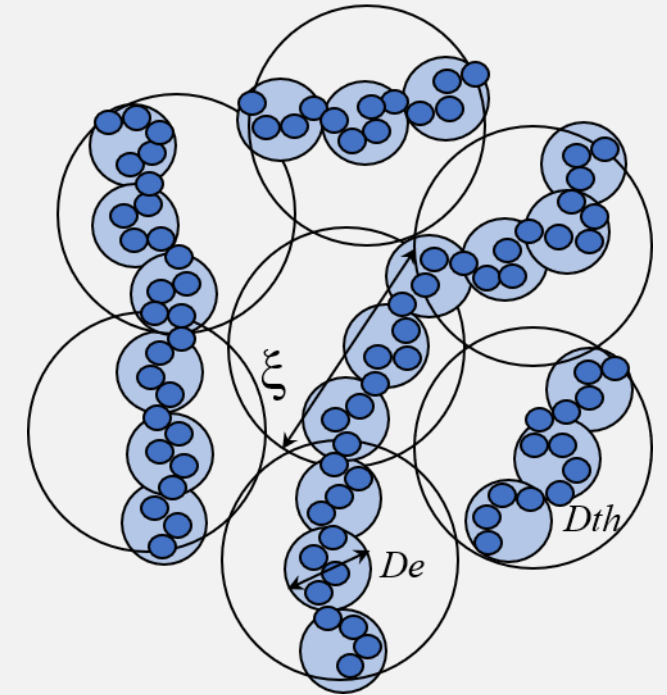
Electrostatic Blob:

$$D_e = D_{th} (g_e / g_{th})^{0.588} = l g_e^{0.588} / B_g$$

Thermal Blob:

$$D_{th} = (l b g_{th})^{0.5} = l g_{th}^{0.5} / B_{th}$$

## Chains of Blobs



$N$  – degree of polymerization  
 $l$  – monomer projection length  
 $b$  – Kuhn length

# Correlation Length

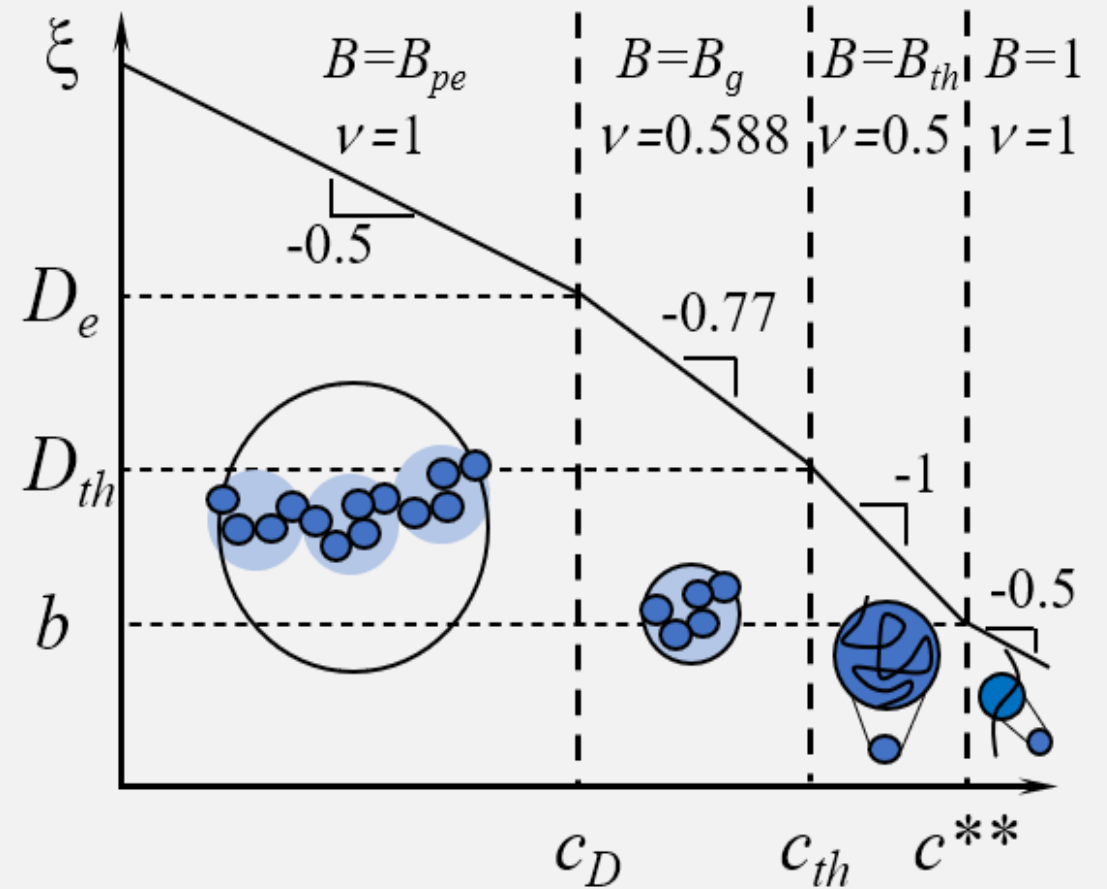
Space-filling blobs

$$\xi = lg^\nu / B$$

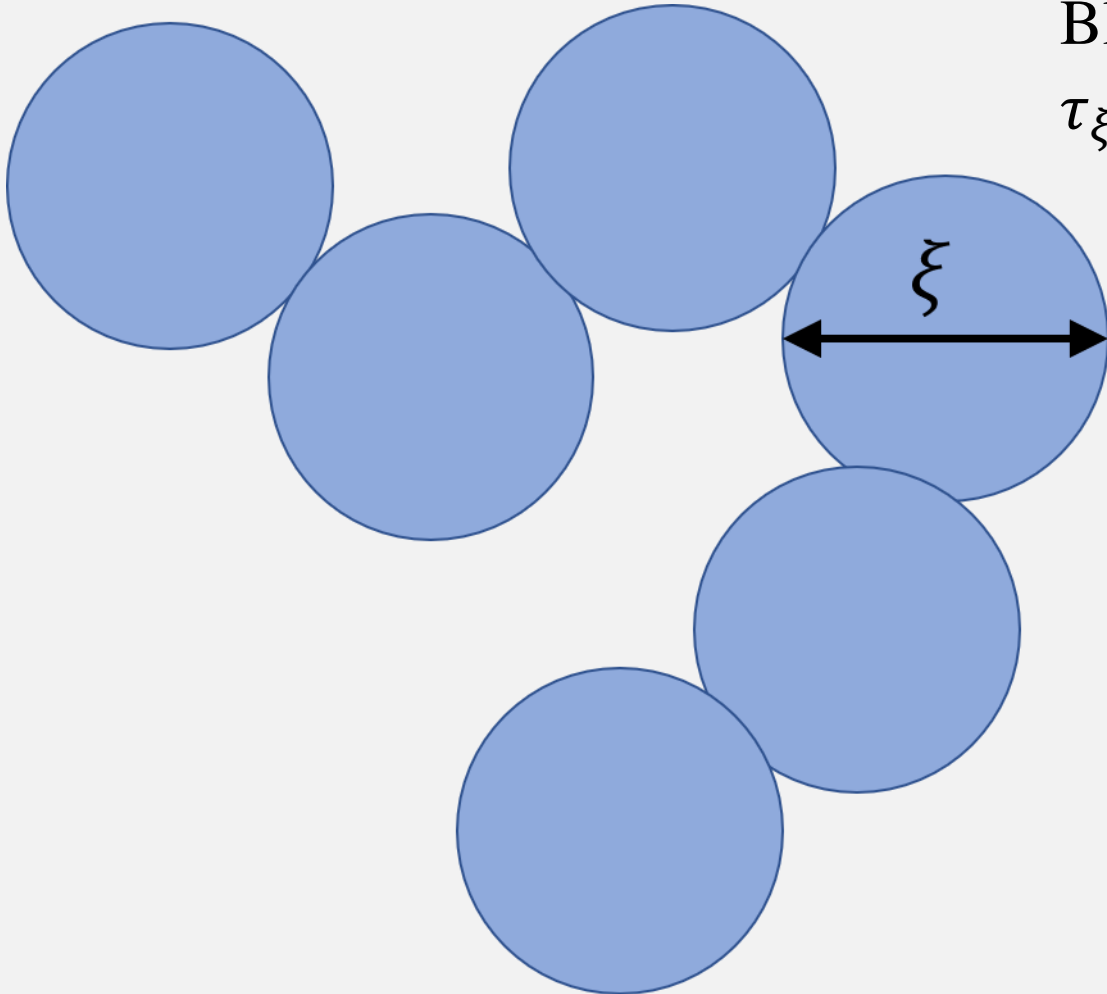
$$g = c\xi^3$$

↓

$$\xi = lB^{1/(3\nu-1)} (cl^3)^{\nu/(1-3\nu)}$$



# Unentangled (Rouse) Dynamics



Blob relaxation time

$$\tau_{\xi} = \frac{\eta_s}{k_B T} \xi^3$$

Longest chain relaxation time

$$\tau_R = \tau_{\xi} \frac{N^2}{g^2} = \frac{\eta_s}{k_B T} \frac{N^2}{g c}$$

Terminal shear modulus

$$G = k_B T c / N$$

Solution viscosity

$$\eta - \eta_s = G \tau_R = \eta_s N / g$$

Specific viscosity

$$\eta_{sp,R} = \frac{N}{g}$$

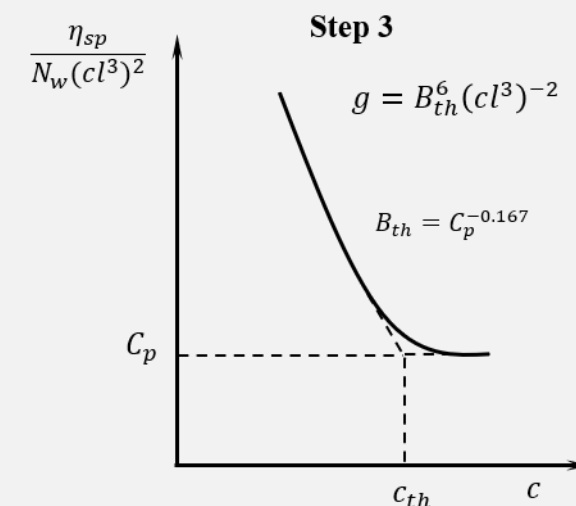
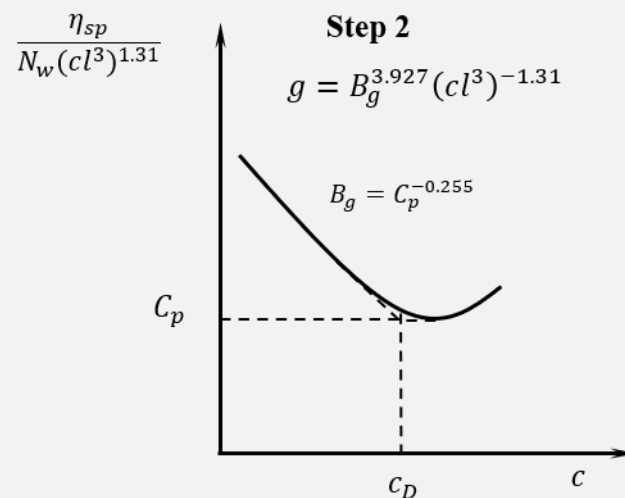
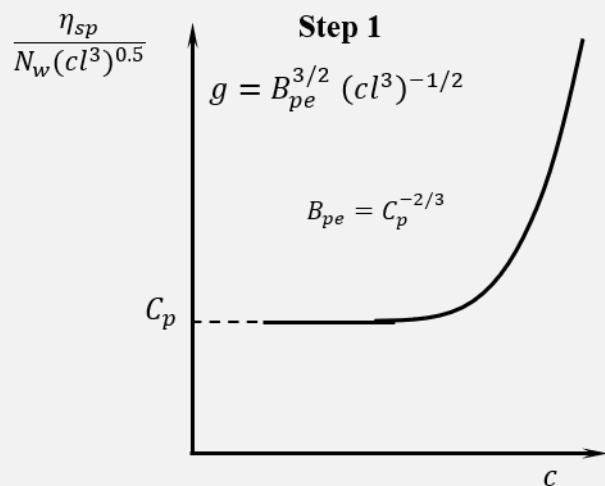
# Viscosity Data Analysis

Polydispersity effect

$$\eta_{sp,R} = N_w/g$$

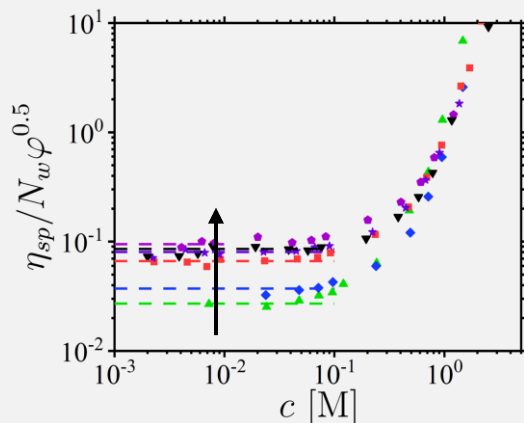
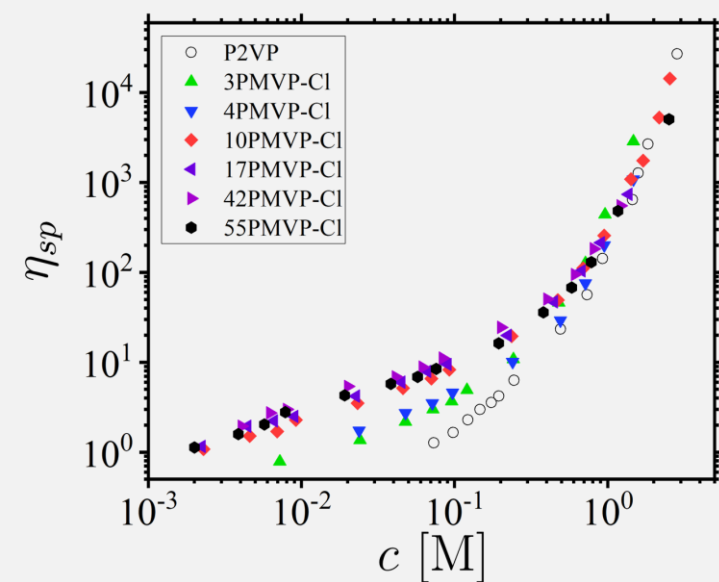
$$g = B^{3/(1-3\nu)} (cl^3)^{1/(3\nu-1)}$$

$$B = C_p^{\frac{1}{3}-\nu}$$

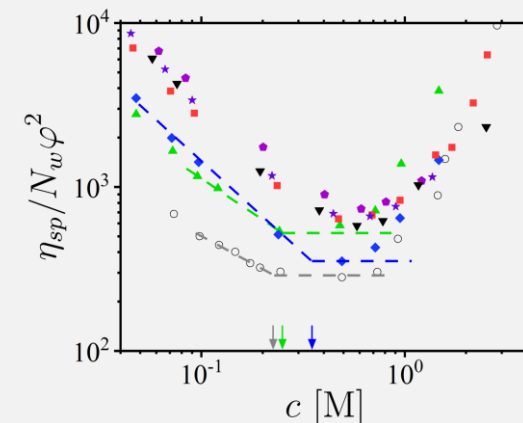
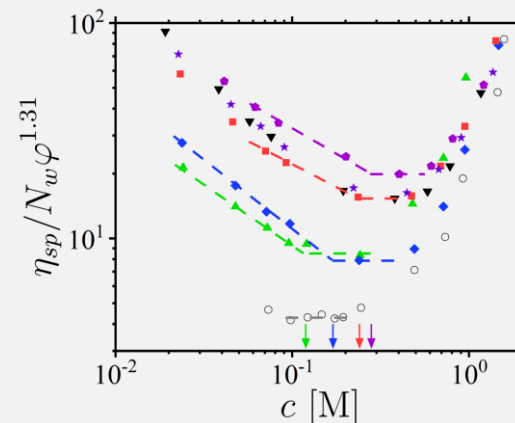


# Salt-free Solutions of PMVP-Cl

Ethylene glycol solutions of P2VP and N-methyl-2-vinyl pyridinium chloride random copolymers with  $N_w = 3463$  and  $l = 0.255\text{nm}$ .



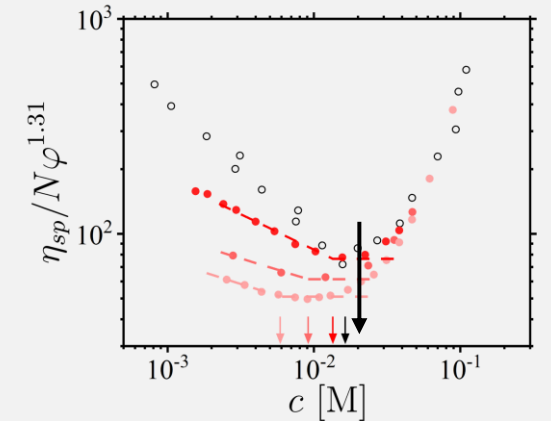
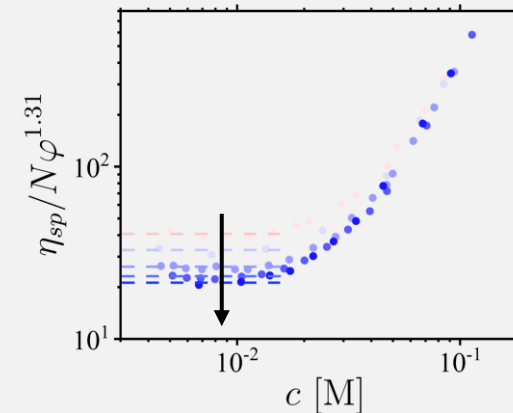
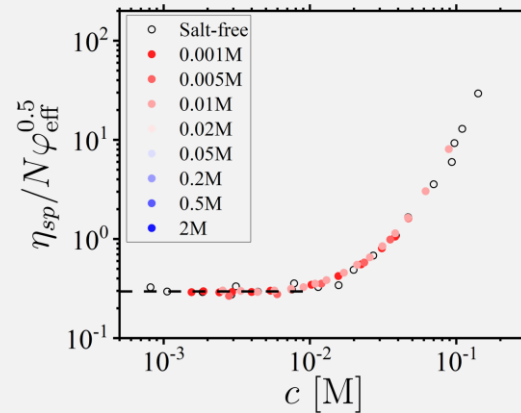
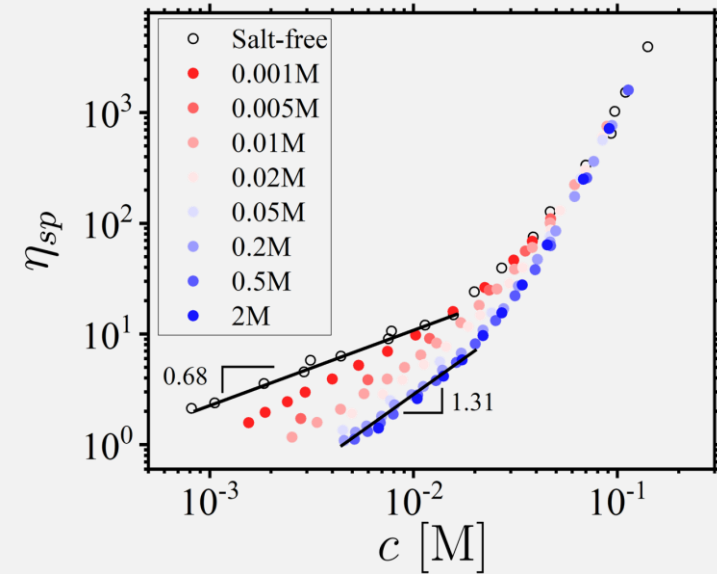
Increasing charge density decreases  $B_{pe}$



$$\varphi = cl^3$$

# Salt Solutions of NaCMC

Aqueous solutions of sodium carboxymethylcellulose with  $N_w = 1250$  and  $l = 0.515\text{nm}$ .



Low salt concentrations:

(*Macromolecules* **1995**, 28, 1859)

$$\xi = l B_{pe}^{0.5} (cl^3)^{-0.5} \left( 1 + \frac{2c_s}{fc} \right)^{0.25}$$

$$\varphi_{\text{eff}}^{0.5} = \varphi^{0.5} (1 + 2c_s / fc)^{-0.75}$$

Residual salt concentration:  $c_s = 4 \times 10^{-4}\text{M}$

Increasing salt concentration increases  $B_g$ .

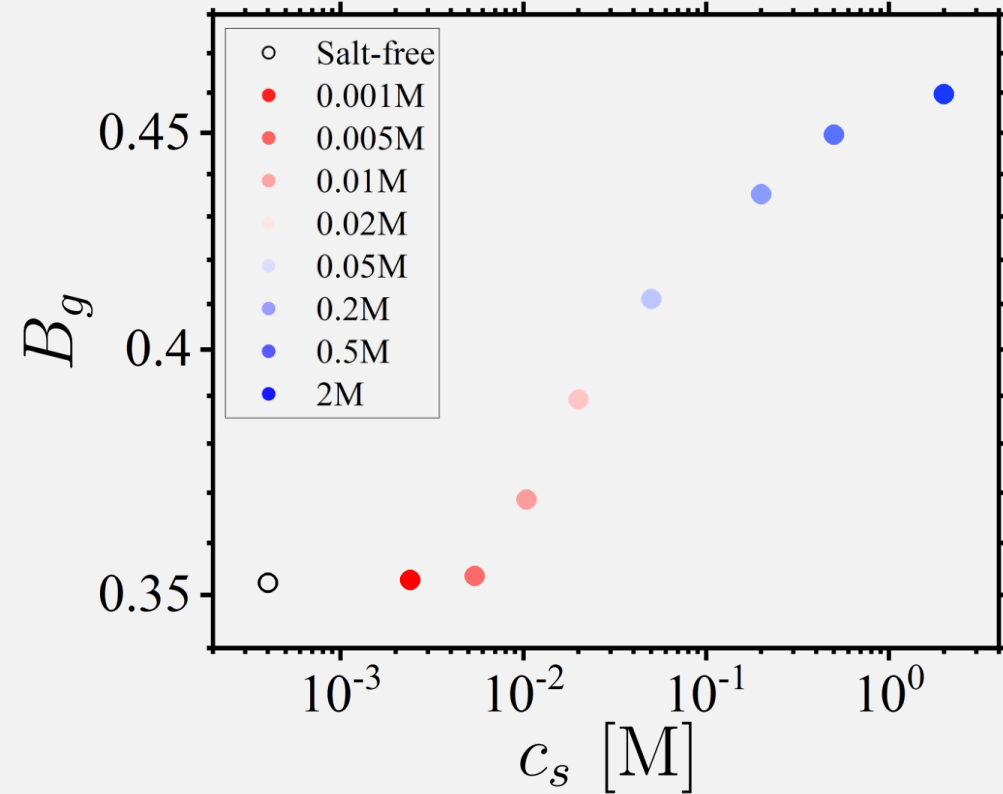
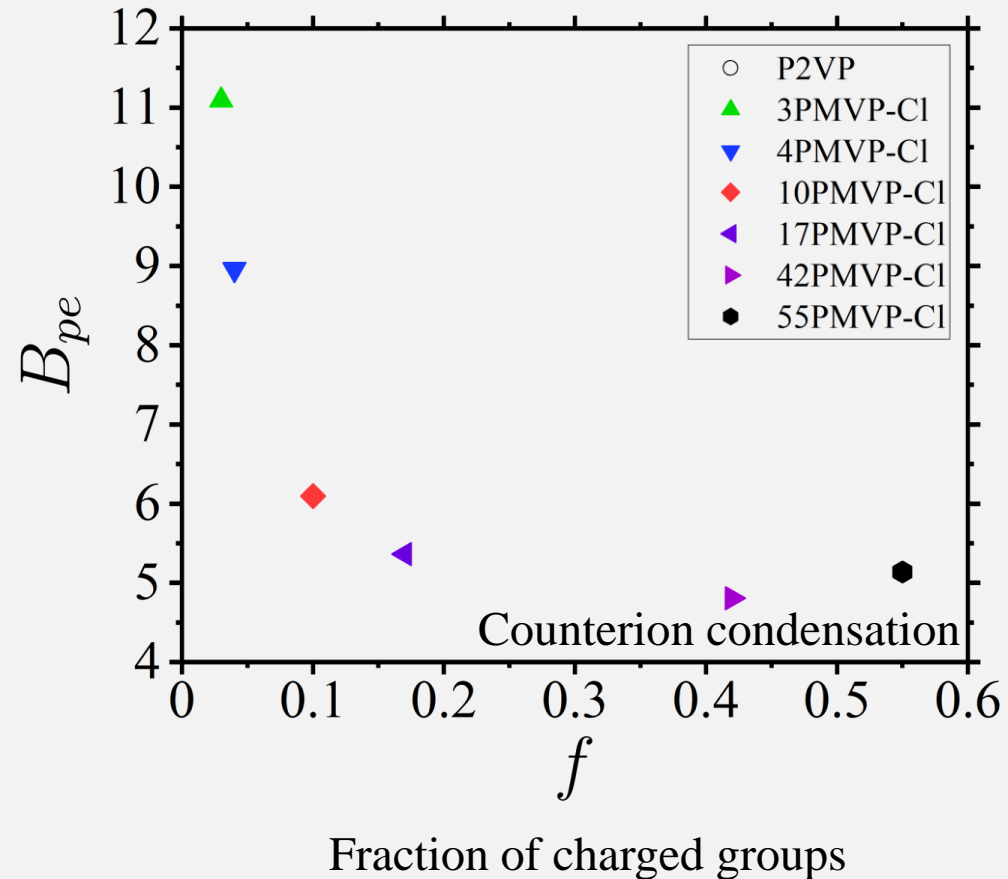
$$\varphi = cl^3$$



# Effect of Fraction of Charged Groups and Salt

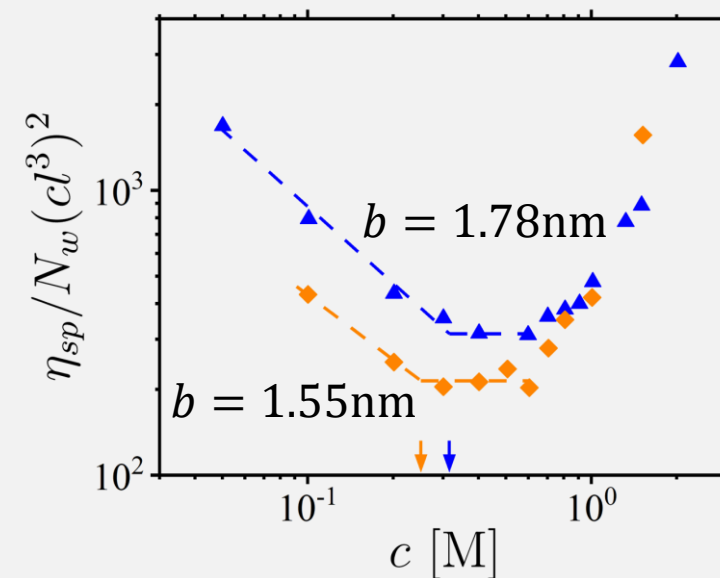
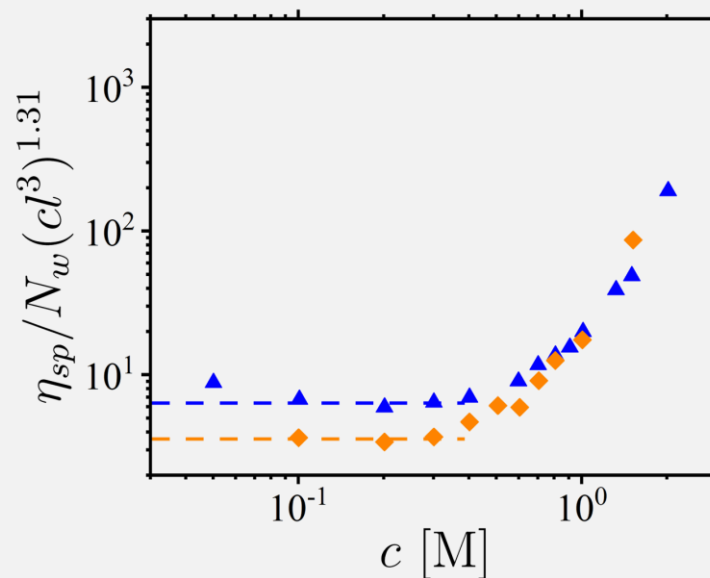
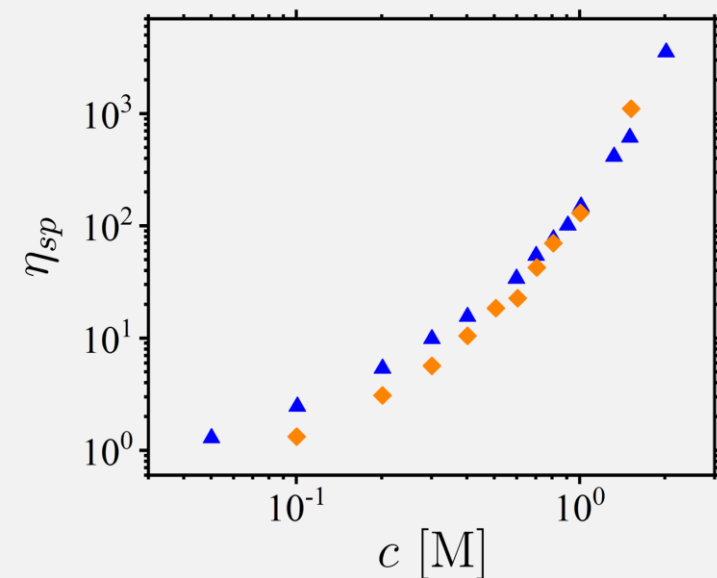
*J. Polym. Sci. B* **2006**, 44, 2001

*Macromolecules* **2016**, 50, 332



# Solutions of PMMA in Ionic Liquids

Solutions of poly(methyl methacrylate) in ionic liquids  $[C_4(\text{mim})][\text{TFSI}]$  (blue triangles) and  $[C_8(\text{mim})_2][\text{TFSI}]_2$  (orange rhombs), with  $N_w = 889$  and  $l = 0.255\text{nm}$ .



Different packing of solvent molecules around the backbone changes  $B_{th}$ , and by extension Kuhn length  $b = lB_{th}^{-2}$ .

# Conclusions

We have adapted the scaling theory of polymer solutions to quantify

- The effect of fraction of ionization on chain size
- The effect of added salt on solvent quality for polyelectrolytes
- The effect of solvent packing on Kuhn length

*And you can too!*

# Acknowledgements

## Collaborators



Andrey V. Dobrynin



Ryan Sayko

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